





Substrate



DNA/RNA are a chain of 4 kinds of bases A, G, C, T/U.

They may *hybridize* with each other primarily by 3 types of base pairs (shown left) between purines (A, G) and pyrimidines (C, T/U).

-- AcGucAu ->

AUGGGU ->

-- AcGucAu ->

Fok1-driven FA terminator а h TIGGCTCGCAGC remaining TGTCGC ACCGAGCGTCG symbols ACAGCG 300 21 Input Fok1 Fok b <S0, a> GGCTCGCAGC **remaining** TGTCGC GCGTCG **symbols** ACAGCG S1 GATGTAC S0 300 22 Transition (T1) Intermediate configuration b Ligase remaining symbols ACAGCG $_{\rm GGT}^{\rm P}$ 22 300 Fokl recognition site Fok gGT 22 GGATGACGAC CCTACTGCTGCCGAp 22 GGATGTAC CCTACATGCCGAP Ligase Fok <\$0. b> T1: S0 \xrightarrow{a} S0 T2: S0 \xrightarrow{a} S1 remaining symbols CAGC 300 GGT 15 GGATGACG GGT 28 GGATGA CCTACTGACCP Next intermediate configuration T5: S1 \xrightarrow{a} S0 T6: S1 \xrightarrow{a} S1 Transition molecules

Atoms of single-stranded RNA structures

Enzyme-driven single-stranded computation

A molecular SAT solver.

- 1. Literals are assigned with DNA sequences in such a way that
 - x and $\neg y$ hybridize with each other iff x = y
 - x and y never hybridize, or neither do $\neg x$ and $\neg y$
- 2. A SAT instance is programmed as a pool made of DNA sequences obtained by choosing one literal from each clause and catenating the corresponding DNA sequences.
- 3. Such a DNA sequence forms a hairpin iff both x and $\neg x$ of a variable are involved.
- 4. A restriction enzyme cuts a hairpin.
- 5. It suffices to check if some DNA sequence has "survived."

Sakamoto et al. Science 288, pp.1223-1226, 2000

RNA co-transcriptionality

Programmable platform for in vitro/vivo computations

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RNA polymerase

Figure 7-7 *Essential Cell Biology* (©Garland Science 2010)

RNA polymerase

The idea of this diagram is from Feynman Lectures on Computation, 1996

Transcripts from a single template in parallel

End

DNA

Begin

RNA origami

architecture for hard-coding a structure into CF

```
int main() {
while (1) {
     std:cout << "Hello RNA World!!";</pre>
return 0;
```

Geary, Rothemund, and Andersen, Science 345 (6198): 799-804, 2014

Helix

co-axial stacking

Helices are stabilized **co-axially** via base-stacking at their interface. Two common motifs involving co-axial stacking are:

RNA origami

mod<mark>ular</mark> design of an RNA tile

Geary, Rothemund, and Andersen, Science 345 (6198): 799-804, 2014

RNA origami

hard-coded CF

Helix

co-axially stacked into a viral backbone

A. van Belkum et al. Nucleic Acids Research 13(21), pp.7673-7686.

RNA sequences are capable of keeping their 3'-end away from their 5'-end, thus,

- folding into non-tree structures, transcending the bound of CFL;
- avoiding to be degraded by ribonuclease (RNase).

Helix

RNA triple helix

RNA Origami to Oritatami

model of CF-driven computing

model of CF-driven computing

The nascent fragment tries to fold with as many bonds as possible.

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model of CF-driven computing

If there are more than one way of fixing H7 point-wise or bond-wise, then **nondeterminism**.

Geary et al. MFCS2016: 43:1-43:14

mod<mark>el o</mark>f CF-driven computing

An oritatami system consists of

- A finite set Σ of types of abstract molecule (*bead*).
- $W \in \Sigma^*$ (transcript)
- $R \subseteq \Sigma \times \Sigma$ (affinity/binding rule)
- δ (*delay*)
- α (*arity*), max # of bonds per bead, formed on the first-come-first-served basis

States by definition!? No! Implement them if needed.

Glider, a self-standing motif

With $\delta = 3$, arbitrary arity $\alpha \ge 1$, $R = \{(a, a'), (b, b')\}$, the periodic transcript a-•-b'-b-•-a'-a-•--- folds into the self-standing *glider* motif.

context-sensitive folding

A transcript can fold differently, depending on what are around (environment).

Terminator stem formation failed (10mM NaF)

Watters et al. Nat. Struct. Mol. Biol. 23(12), pp.1124-1131, 2016

context-sensitive folding

A transcript can fold differently, depending on what are around (environment).

context-sensitive folding

A transcript can fold differently, depending on what are around (environment).

(F0)

(F1)

(F2)

(F3)

(F4)

(F5)

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Complex structures are often made of simple identical (homo-) units (polymers) in nature.

A periodic RNA transcript (homo-polymer) can be transcribed from a circular DNA.

Homo-polymeric CF-driven computing

Zigzag binary counter

- The first oritatami implementation
- Fixed bit-width (3 in the right figure), but later endowed with capability to widen by 1 bit at every overflow
- A transcript is of period 60 as 0-1---- 11-12----29-30----41-42-----59-0-1-----.
- Increment by 1 per zigzag.
- The factors 0----11 and 30----41 serve as a half-adder by folding into one of 4 possible conformations, depending on what are around.

Homo-polymeric CF-driven computing

Turing-universality

- Cyclic tag system (cts) is a binary rewriting system made of a cyclic list of $u_0, u_1, \dots, u_{k-1} \in \{0, 1\}^*$ and a pointer $0 \le p < k$. It rewrites a word $w = a_1 a_2 \cdots a_n$ as:
 - 1. temp = $a_2 \cdots a_n$ (a_1 is deleted from w)
 - 2. If $a_1 = 1$, temp = temp u_p
 - *3. w* = temp
 - *4. p*++ (mod *k*)

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Homo-polymeric CF-driven computing

Tessellation by a transcript of period 37 at delay 3

Turedo (Tur[-ing] + [Ter-]edo [navilis]) Programming language for CF

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- 2D Turing machine on the hex grid that is *self-avoiding*, that is,
- Once visited, a cell won't be visited again.
- According to the configuration within the radius-r from its head, it colors the current cell and decides which neighbor to visit next, where r is a system parameter.

Example of radius-1 Turedo (mod-4 clockwise walker)

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2D Turing machine on the hex grid that is *self-avoiding*, that is,

- Once visited, a cell won't be visited again.
- According to the configuration within the radius-r from its head, it colors the current cell and decides which neighbor to visit next, where r is a system parameter.

- A radius-1 stateless Turedo $T = (A, \delta)$ is a pair of a tape alphabet A including the blank \perp and a transition function $\delta: A^6 \rightarrow A \times \{BR, FR, S, FL, BL\}.$
- Suppose *T* has come from north, where x_5 is written. If $\delta(q, x_0, x_1, x_2, x_3, x_4, x_5) = (a, d)$, then it
 - 1. writes $a \in A$ at the current cell, and
 - moves to the neighbor cell in the direction d, <u>as long as the cell is still blank</u>; otherwise, it halts.

Turedo-to-Oritatami Compiler Theorem.

A radius-1 stateless Turedo $T = (A, \delta)$ can be programmed into a transcript w of period $O(|A|^6 \log |A|)$ with which the deterministic delay-3 oritatami system ($\Sigma, w, R, 3, 6$) simulates T intrinsically, where

- Σ is universal, that is, independent of *T*, and consists of 1753 bead types.
- *R* is also universal.
- Each period of w folds into a macrocell of side length $O(|A|^3 \log |A|)$.

Macrocell

- 1. Scaffold layer
- 2. Read (log|A| bits/side) layer
- 3. Write (log|A| bits/side) layer
- 4. Exit layer

 $O(|A|^3 \log|A|)$

Shift-driven computing

Period of transcript

A Turedo $T = (A, \delta)$ is encoded in the period of a transcript as:

Scaffold \rightarrow **Read** \rightarrow **Write** \rightarrow **Speedbump** \rightarrow **Exit** \rightarrow **Scaffold** \rightarrow \cdots

Scaffold hardcodes the macrocell's skeleton

Read $x = (x_0, x_1, x_2, x_3, x_4, x_5)$ with $x_s = (b_{s,0}, b_{s,1}, \dots, b_{s,\log|A|-1})$

• Weigh-sums the bits in $x_0, x_1, \dots x_5$ in this order as:

$$\Delta(x) = \sum_{s=0}^{5} \sum_{i=0}^{\log|A|-1} b_{s,i} 2^{s\log|A|+i}$$

• Pushes the remaining transcript forward by this offset.

NOTE. these bits must have been written in a **uniform** format. It is uncomputable whether a cell will be visited; let alone from which direction it will be entered.

 $x_{\!5}$

 x_2

 x_0

 x_1

 x_4

 x_3

Read **5**: Reading pockets

OK, readers, it's you who weighs bits!!

Otherwise

Read U: Reading pockets

If the *j*-th bit is 1, then $\Delta(x) += 2^{s\log|A|+j}$

Period of transcript

A Turedo $T = (A, \delta)$ is encoded in the period of a transcript as:

Scaffold \rightarrow **Read** \rightarrow **Write** \rightarrow **Speedbump** \rightarrow **Exit** \rightarrow **Scaffold** $\rightarrow \cdots$

Write a and d (letter & direction)

- All the transition tables for each bit and for exit-direction are encoded: |A|⁶ entries per table.
- This layer is shifted by $\Delta(x)$ so that only the referred entry by x of each table is exposed at a position readable later while the others are "hidden."
- Outputs must be in a uniform format along all the sides.

Speedbump absorbs $\Delta(x)$

Exit at the side d(x) specified by Write

 x_5

 x_2

 x_0

 x_1

 x_4

 x_3

Read U to Write U: U-turn pocket

The shift is transferred from **Read** to **Write**.

Write \mathbf{U} : tables shifted by $\Delta(x)$

NOTE: The system knows in the stage of programming tables for each x, whether each bit will be covered by Exit according to the exit direction d(x).

"Foldable" Speedbump: absorbing $\Delta(x)$

Based on the straight speedbump [PchelinaSSU20] but quadratically more spaceefficient.

RNA Spinner

In vitro/vivo auto-synthesis of RNA components by NFA

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 $uxs\ell\theta(s)yv \rightarrow uv$ if

Co-transcriptional splicing

- (x, y) is an enzymatically-recognizable context and
- 2. $s\ell\theta(s)$ is a *stable* hairpin, where θ is an antimorphic involution.

An NFA for a *superset* of *R*.

RNA spinner

Circular O DNA

Co-transcriptional

splicing

encoding

oxdry.

Any molecular system consists of *finitely many* (*kinds*) of DNA and RNA sequences. Let *R* be the *finite* set of RNA sequences it involves.

Recall that RNAs are naturally degraded.

 $y_{0}a\overrightarrow{x_{0}} \cdot y_{0}bx_{1} \cdot y_{1}ax_{1} \cdot y_{1}bx_{0} - \overleftarrow{y_{0}}ax_{0} \cdot y_{0}bx_{1} \cdots$ $\rightarrow \qquad y_{0}aa\overrightarrow{x_{0}} \cdot \overleftarrow{y_{0}}bx_{1} \cdot y_{1}ax_{1} \cdots$ $\rightarrow \qquad y_{0}aabx_{1} \cdot y_{1}ax_{1} \cdots$

Problems to be solved for RNA Spinner

Problem 1.

Given *R* and a finite set *D* of domains (via which sequences in *R* interact with each other or with other molecules), construct an NFA *A* with as *few transitions* as possible s.t.

$R \subseteq L(A) \subseteq R \cup \overline{\Sigma^* D \Sigma^*}$

By setting $D = \Sigma$, this problem is reduced to the NP-hard problem of finding a transition-minimal NFA for finite languages [GruberH07]. Such a ubiquitous domain however turns any system into a chaotic soup.

Problems to be solved for RNA Spinner

A hairpin gets less stable with a longer loop and a shorter stem.

Contribution by stem is linear, while it remains open how a loop is penalized.

Problem 2

Propose a proper energy model for RNA hairpin stability, and study hairpin-related operations by considering only stable hairpins in the model.

ble 6. Free-energy increments for loops			
Loop size	Internal loop*†	Bulge loop* [‡]	Hairpin loop ^{*§}
1		+3.3	_
2	+0.8	+5.2	_
3	+1.3	+6.0	+7.4
4	+1.7	+6.7	+5.9
5	+2.1	+7.4	+4.4
6	+2.5	+8.2	+4.3
7	+2.6	+9.1	+4.1
8	+2.8	+10.0	+4.1
9	+3.1	+10.5	+4.2
10	+3.6	+11.0	+4.3
12	+4.4	+11.8	+4.9
14	+5.1	+12.5	+5.6
16	+5.6	+13.0	+6.1
18	+6.2	+13.6	+6.7
20	+6.6	+14.0	+7.1
25	+7.6	+15.0	+8.1
30	+8.4	+15.8	+8.9

Freier et al., *PNAS* 83, pp.9373-9377, 1986

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